

NUMERICAL PROBLEMS

15.1 A transformer is needed to convert a mains 240 V supply into a 12V supply. If there are 2000 turns on the primary coil, then find the number of turns on the secondary coil.

Solution:

Given Data:

$$V_p = 240 \text{ V}$$

$$V_s = 12 \text{ V}$$

$$N_p = 2000$$

Required: $N_s = ?$

Formula:

$$\frac{N_s}{N_p} = \frac{V_s}{V_p}$$

$$N_s = \frac{V_s \times N_p}{V_p} = \frac{12 \times 2000}{240} = 100$$

15.2 A step-up transformer has a turn ratios of 1:100. An alternating supply of 20V is connected across the primary coil. What is secondary voltage?

Solution:

Given Data:

$$N_p : N_s = 1 : 100$$

$$V_p = 20 \text{ V}$$

Required :

$$V_s = ?$$

Formula

$$\frac{N_p}{N_s} = \frac{1}{100}$$

$$\frac{V_s}{V_p} = \frac{N_s}{N_p}$$

$$V_s = \frac{N_s \times V_p}{N_p} = \frac{100}{1} \times 20$$

$$V_s = 2000 \text{ Volt} \quad \text{Ans}$$

- 15.3 A step – down transformer has a turns ratio of 1:100. An ac voltage of amplitude 170V is applied to the primary. If the current in the primary is 10 mA, what is the current in the secondary?

Solution:

Given Data:

$$N_s : N_p = 1 : 100$$

$$\frac{N_s}{N_p} = \frac{1}{100}$$

$$V_p = 170\text{v}$$

$$I_p = 1\text{mA} = 1 \times 10^{-3} \text{ A}$$

Required

$$I_s = ?$$

Formula

$$\frac{V_s}{V_p} = \frac{N_s}{N_p}$$

$$V_s = \frac{N_s}{N_p} \times V_p$$

$$= \frac{1}{100} \times 170 = 1.7\text{V}$$

For an ideal transformer

Power of primary = Power of secondary

$$P_p = P_s$$

$$I_p V_p = I_s V_s$$

$$\frac{I_p V_p}{V_s} = I_s$$

$$\frac{1 \times 10^{-3} \times 170}{1.7} = I_s$$

$$0.1 \text{ A} = I_s \Rightarrow I_s = 0.1 \text{ A Ans}$$

- 15.4 A transformer, designed to convert the voltage from 240 V a.c. mains to 12V, has 4000 turns on the primary coil. How many turns should be on the secondary coil? If the transformer were 100% efficient, what current would flow through the primary coil when the current in the secondary coil was 0.4A?

Solution:

Given Data:

$$V_p = 240\text{V}$$

$$V_s = 12\text{V}$$

$$N_p = 4000$$

Required: $N_s = ?$

Formula:

$$\frac{N_s}{N_p} = \frac{V_s}{V_p}$$

$$N_s = \frac{V_s \times N_p}{V_p} = \frac{12 \times 4000}{240}$$

$$N_s = 200 \text{ Ans}$$

$$I_p = ?$$

$$I_s = 0.4 \text{ A}$$

$$P_p = P_s$$

$$I_p V_p = I_s V_s$$

$$I_p = \frac{I_s V_s}{V_p} = \frac{0.4 \times 12}{240}$$

$$I_p = 0.02 \text{ A}$$

15.5 A power station generates 500 MW of electrical power which is fed to a transmission line. What current would flow in the transmission line if the input voltage is 250 kV?

Solution:

Given Data:

$$V = 250 \times 10^3 \text{ V}$$

$$\text{Power} = P = 500 \times 10^6 \text{ W}$$

Required: $I = ?$

Formula: $P = IV$

$$\frac{P}{V} = I$$

$$\frac{500 \times 10^6}{250 \times 10^3} = I$$

$$2 \times 10^3 \text{ A} = I \Rightarrow I = 2 \text{ KA Ans}$$

15.6 The diagram shows a wind turbine which a 150 kW generator with an output voltage of 1000V. The voltage is increased by transformer T_1 to 10 000 V for transmission to a town 5 km away through power lines with a total resistance of 2Ω . Another transformer, T_2 , at the town reduces the voltage to 250V. Assume that the transformers are 'Ideal' when the system is running at full power: (Figure from the textbook page 143)

Solution:

Given Data:

$$\text{Power} = P = 150 \text{ k W}$$

$$P = 150 \times 10^3 \text{ W}$$

$$\text{At } T_1 \quad V_p = 10000 \text{ V}$$

$$R = 2\Omega$$

$$\text{At } T_2 \quad V_s = 250$$